Mechanized Proofs of Adversarial Complexity and Application to Universal Composability

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Cryptographic Reduction $\mathcal{S} \leq_{\mathsf{red}} \mathcal{H}$

 ${\mathcal S}$ reduces to a hardness hypothesis ${\mathcal H}$ (e.g. DLog, DDH) if:

 $\forall \mathcal{A}. \exists \mathcal{B}. \ \mathsf{adv}_{\mathcal{S}}(\mathcal{A}) \leq \mathsf{adv}_{\mathcal{H}}(\mathcal{B}) + \epsilon \ \land \ \mathsf{cost}(\mathcal{B}) \leq \mathsf{cost}(\mathcal{A}) + \delta$

where ϵ and δ are small.

Advantage of an unbounded adversary is often 1. \Rightarrow bounding \mathcal{B} 's resources is critical **EASYCRYPT** is a **proof assistant** to verify cryptographic proofs. In the proof, the adversary against \mathcal{H} is **explicitly constructed**:

$$\forall \mathcal{A}. \ \mathsf{adv}_{\mathcal{S}}(\mathcal{A}) \leq \mathsf{adv}_{\mathcal{H}}(\mathcal{C}[\mathcal{A}]) + \epsilon \tag{\dagger}$$

But EASYCRYPT lacked support for complexity upper-bounds.

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But EASYCRYPT lacked support for complexity upper-bounds.

Getting a $\forall \exists$ **statement**

(†) implies that:

$$\forall \mathcal{A}. \exists \mathcal{B}. adv_{\mathcal{S}}(\mathcal{A}) \leq adv_{\mathcal{H}}(\mathcal{B}) + \epsilon$$

but this statement is **useless**, since \mathcal{B} is not resource-limited: its advantage is often 1.

Hence adversaries **constructed** in reductions are kept **explicit**:

```
\forall \mathcal{A}. adv_{\mathcal{S}}(\mathcal{A}) \leq adv_{\mathcal{H}}(\mathcal{C}[\mathcal{A}]) + \epsilon
```

Limitations

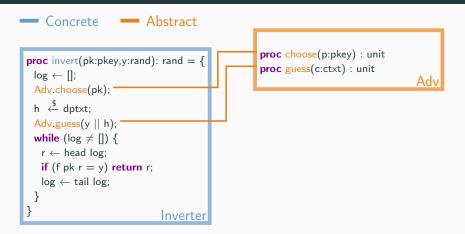
- Not fully verified: C[A]'s complexity is checked manually.
- Less composable, as composition is done manually (inlining).

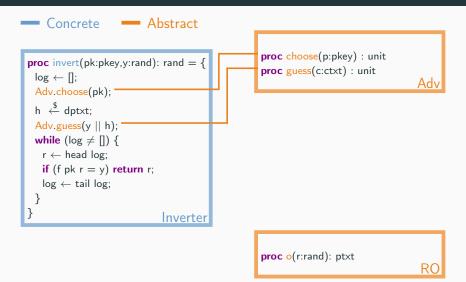
If
$$\forall \mathcal{A}. adv_{\mathcal{S}}(\mathcal{A}) \leq adv_{\mathcal{H}_1}(\mathcal{C}[\mathcal{A}]) + \epsilon_1$$

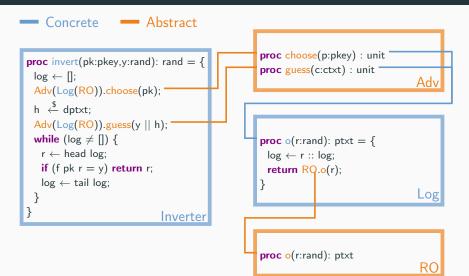
- and $\forall \mathcal{D}. adv_{\mathcal{H}_1}(\mathcal{D}) \leq adv_{\mathcal{H}_2}(\mathcal{F}[\mathcal{D}]) + \epsilon_2$
- then $\forall \mathcal{A}. adv_{\mathcal{S}}(\mathcal{A}) \leq adv_{\mathcal{H}_2}(\mathcal{F}[\mathcal{C}[\mathcal{A}]]) + \epsilon_1 + \epsilon_2$

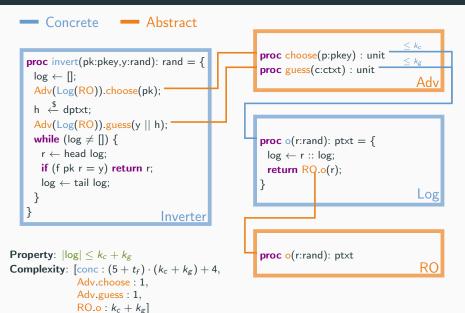
- A Hoare logic to prove worst-case complexity upper-bounds of probabilistic programs.
 - ⇒ fully mechanized cryptographic reductions.
- Implemented in EASYCRYPT, embedded in its ambient higher-order logic.
 - \Rightarrow meaningful $\forall \exists$ statements: better **composability**.
- Application: UC formalization in EASYCRYPT.
- First formalization of EASYCRYPT module system. (of independent interest)

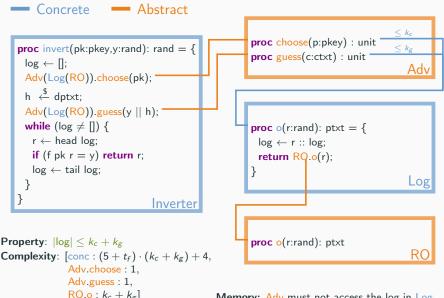
Hoare Logic for Complexity











Memory: Adv must not access the log in Log 5

- Support programs mixing concrete and abstract code.
 Example: Adv(Log(RO))
- Complexity upper-bound requires some program invariants. Example: |log| ≤ k_c + k_g

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Abstract procedures must be restricted:

- Complexity: restrict intrinsic cost/number of calls to oracles. Example: choose can call o ≤ k_c times.
- Memory footprint: some memory areas are off-limit.
 Example: Adv cannot access the log in Log's memory

Abstract code modeled as any program implementing some module signature (à la ML)

```
module type RO = {
  proc o (r:rand) : ptxt
}.
module type Adv (H: RO) = {
  proc choose(p:pkey) : unit
  proc guess(c:ctxt) : unit
```

}.

Abstract code modeled as any program implementing some module signature (à la ML), with some restrictions:

Module memory footprint can be restricted.

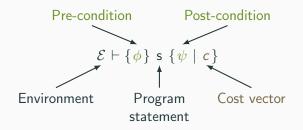
```
module type RO = {
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}.
```

Abstract code modeled as any program implementing some module signature (à la ML), with some restrictions:

- Module memory footprint can be restricted.
- Procedure complexity can be upper-bounded.

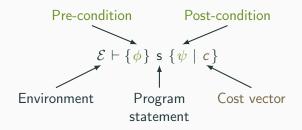
```
module type RO = {
  proc o (r:rand) : ptxt [intr : t_o]
}.
module type Adv (H: RO) {+all mem, -Log, -RO, -Inverter} = {
  proc choose(p:pkey) : unit [intr : t_c, H.o : k_c]
  proc guess(c:ctxt) : unit [intr : t_g, H.o : k_g]
}.
```

Complexity Judgements



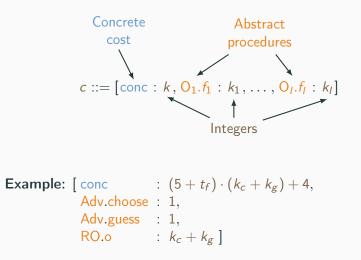
Assuming ϕ , evaluating s guarantees ψ , and takes time at most c.

Complexity Judgements



Assuming ϕ , evaluating s guarantees ψ , and takes time at most c.

Example: $\mathcal{E} \vdash \{\top\}$ Inverter(Adv,RO).invert $\{|\log| \le k_c + k_g \mid c\}$



 \mathbf{IF}

$$\begin{array}{l} \vdash \{\phi\} \ e \leq t_e \\ \mathcal{E} \vdash \{\phi \land e\} \ \mathsf{s}_1 \ \{\psi \mid t\} & \mathcal{E} \vdash \{\phi \land \neg e\} \ \mathsf{s}_2 \ \{\psi \mid t\} \\ \hline \mathcal{E} \vdash \{\phi\} \ \mathsf{if} \ e \ \mathsf{then} \ \mathsf{s}_1 \ \mathsf{else} \ \mathsf{s}_2 \ \{\psi \mid t + t_e\} \end{array}$$

Whenever:

- e takes time $\leq t_e$;
- **s**₁, assuming $\phi \wedge e$, guarantees ψ in time $\leq t$;

■ s₂, assuming $\phi \land \neg e$, guarantees ψ in time $\leq t$; then the conditional, assuming ϕ , guarantees ψ in time $\leq t + t_e$.

Hoare Logic for Cost

 $\mathcal{E} \vdash \{d'\} \times \{\psi' \mid t'\}$ $\phi \Rightarrow \phi' \quad \psi' \Rightarrow \psi \quad t' \leq t$ 8 ⊢ {φ̂} skip {φ̂ | 0} $(t | \psi) \ge (\phi + 3)$ Assign $\vdash {\phi} c \leq t_e$ $\mathcal{E} \models \{\phi \land \psi[x \leftarrow e]\} x \leftarrow e \{\psi \mid I_e\}$ $\vdash \{\phi_0\} d \leq t$ $\mathcal{E} \vdash \{\phi\} \leq \{\phi' \mid I_1\}$ $\phi = (\phi_0 \land \forall v \in \operatorname{dom}(d), \phi[x \leftarrow v])$ $\mathcal{E} \vdash \{\phi'\} = \{\psi \mid t_2\}$ $\mathcal{E} \vdash \{\phi\} x \stackrel{s}{\leftarrow} d \{\psi \mid t\}$ $\mathcal{E} \vdash \{\phi \land e\} \leq \{\psi \mid t\}$ $\mathcal{E} \vdash \{\phi \land \neg e\} \cong \{\phi \mid t\} \vdash \{\phi\} e \leq L$ $\mathcal{E} \vdash \{\phi\}$ if c then s, else s, $\{\psi \mid t + t_n\}$ Winne $I \land e \Rightarrow c \leq N$ $\forall k, E \vdash \{I \land e \land c = k\} \in \{I \land k < c \mid t(k)\}$ $\forall k \le N, \vdash \{I \land e \land c = k\} \ e \le t_e(k) \qquad \vdash \{I \land \neg e\} \ e \le t_e(N+1)$ $\mathcal{E} \models \{I \land 0 \le c\}$ while e dos $\{I \land \neg e \mid \sum_{i=a}^{N} t(i) + \sum_{i=a}^{N+1} t_e(i)\}$ $\operatorname{args}_{v}(F) = \vec{v} + \{\phi | \vec{v} \leftarrow \vec{e} \} \in \{t_{v} \in V\}$ $\mathcal{E} \vdash {\phi} F {\psi[x \leftarrow ret] \mid t}$ $\mathcal{E} \vdash \{\phi | \vec{v} \leftarrow \vec{e} \} x \leftarrow \text{call } F(\vec{e}) \{\psi \mid t_e + t\}$ CON f-resc(F) = (proc $f(\vec{y}:\vec{\tau}) \rightarrow \tau_r = \{:s: return r \}$) $\mathcal{E} \vdash \{\phi\} \in \{\psi | ret \leftarrow r\} \mid t\} \vdash \{\psi\} r \leq t_{ret}$ Convention: ret cannot appear in programs (i.e. ret & V). Figure 22: Basic rules for cost judgment.

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$$\begin{split} & \int trang(f) = the long are u(f) f \\ & f(x) = the long are u(f) f(x) = the long are u(f) \\ & f(x) = the long are u(f) = the long are u(f) \\ & f(x) = the long are u(f) = the long$$

Conventions: $\vec{\gamma}$ can be empty (this corresponds to the non-functor case).

Figure 6: Abstract call rule for cost judgment.

 $\begin{array}{l} \begin{array}{l} \mbox{DISTANTIATION} \\ M_{p} = func(\vec{y} \cdot \vec{M}) \sin S_{1} \operatorname{rest} r \theta \mbox{ end} \\ \vec{E} \vdash_{e} m : \operatorname{erase}_{comp}(M_{e}) & \overline{r} \mbox{ fresh in } \mathcal{E} \\ \end{tabular} \\ \end{tabular} \quad \end{tabular} \\ \end{tabular} \quad \end{tabular} \\ \end{tabular} \quad \end{tabular} \quad \end{tabular} \quad \end{tabular} \quad \end{tabular} \\ \end{tabular} \quad \end{tabular} \quad \end{tabular} \quad \end{tabular} \quad \end{tabular} \\ \end{tabular} \quad \end{tabu$

where:

 $T_{ins} = \{G \mapsto t_s[G] + \sum_{f \in procs(S_i)} t_s[x, f] \cdot t_f[G]\}$

 $t_f \leq_{\text{compl}} \theta[f] = \forall z_0 \in \vec{z}, \forall g \in \text{procs}(\vec{M}[z_0]), t_f[z_0,g] \leq \theta[f][z_0,g] \land t_f[\text{conc}] + \sum_{\substack{A \in \text{abs}(\mathcal{E}) \\ h \in \text{procs}_f(A)}} t_f[A,h] \cdot \text{int}_{\mathcal{E}}(A,h) \leq \theta[f][\text{intr}]$

Conventions: $intr_{\mathcal{E}}(A, h)$ is the intr field in the complexity restriction of the abstract module procedure A, h in \mathcal{E} .

Figure 23: Instantiation rule for cost judgment.

Hoare logic for cost

Rules handling abstract code are the most interesting.

Hoare Logic for Cost

 $\mathcal{E} \vdash \{ \hat{\alpha}' \} \times \{ \psi' \mid I' \}$ $\phi \Rightarrow \phi' \quad \psi' \Rightarrow \psi \quad t' \leq t$ 8 ⊢ {φ̂} skip {φ̂ | 0} $(t | \psi) \ge (\phi + 3)$ $\vdash {\phi} c \leq t_e$ $\mathcal{E} \models \{\phi \land \psi[x \leftarrow e]\} x \leftarrow e \{\psi \mid I_e\}$ $\vdash \{\phi_0\} d \leq t$ $\mathcal{E} \vdash \{\phi\} \leq_1 \{\phi' \mid t_1\}$ $\phi = (\phi_0 \land \forall v \in \operatorname{dom}(d), \phi[x \leftarrow v])$ $\mathcal{E} \vdash \{\phi'\} = \{\psi \mid t_2\}$ $\mathcal{E} \vdash \{\phi\} x \stackrel{s}{\leftarrow} d \{\psi \mid t\}$ $\mathcal{E} \vdash \{\phi \land e\} \leq \{\psi \mid t\}$ $\mathcal{E} \models (\phi \land \neg e) \Rightarrow (\phi \mid t) \models (\phi) e \leq t_e$ $\mathcal{E} \vdash \{\phi\}$ if c then s, else s, $\{\psi \mid t + t_n\}$ Winne $I \land e \Rightarrow c \le N$ $\forall k, E \vdash \{I \land e \land c = k\} \in \{I \land k < c \mid t(k)\}$ $\forall k \le N, \vdash \{I \land e \land c = k\} \ e \le t_e(k) \qquad \vdash \{I \land \neg e\} \ e \le t_e(N+1)$ $\mathcal{E} \vdash \{I \land 0 \le c\}$ while c do $s \{I \land \neg c \mid \sum_{i=1}^{N} t(i) + \sum_{i=1}^{N+1} t_{c}(i)\}$ $\operatorname{args}_{\mathcal{C}}(F) = \vec{v} + (\phi | \vec{v} \leftarrow \vec{e} |) \vec{e} \le t_e$ $\mathcal{E} \vdash {\phi} F {\psi[x \leftarrow ret] \mid t}$ $\mathcal{E} \vdash \{\phi | \vec{v} \leftarrow \vec{e} \} x \leftarrow \text{call } F(\vec{e}) \{\psi \mid t_e + t\}$ CON f-resc(F) = (proc $f(\vec{y}:\vec{\tau}) \rightarrow \tau_r = \{:s: return r \}$) $\mathcal{E} \vdash \{\phi\} \in \{\psi | ret \leftarrow r\} \mid t\} \vdash \{\psi\} r \leq t_{ret}$ Convention: ret cannot appear in programs (i.e. ret & V). Figure 22: Basic rules for cost judgment.

ABS

$$\begin{split} & \{ \operatorname{sensel} f = (\operatorname{sensen} x) \{ f \} \in (\operatorname{sensen} x) \{ f \}, f \\ & \mathcal{E}(x) = \operatorname{sensen} x: (\operatorname{sensen} x) : \operatorname{sensen} x = \operatorname{sensen} x \\ & \mathcal{O}[f] = \lambda_m, A_n + \lambda_n + \alpha : \operatorname{comp}[f] : x : K_{21}, f_1 : K_{21}, \dots, x_{21}, f_1 : K_1] \\ & \quad = \operatorname{comp}[f] : x : K_{21}, f_1 : K_1 = X_1 + \alpha : K_{21}, f_1 : K_1 + \alpha : K_{21}, f_1 : K_1 + \alpha :$$

where $T_{abs} = \{x, f \mapsto 1; (G \mapsto \sum_{l=1}^{l} \sum_{k=0}^{K_l-1} (t_l \ k)[G])_{Grs, f}\}$ Conventions: \vec{x} can be empty (this corresponds to the non-functor case).

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Figure 6: Abstract call rule for cost judgment.

$\begin{array}{c} \begin{array}{l} \text{INSTANTIATION} \\ M_{1} = func(\overline{y}: \widetilde{M}) & \text{sig} \; S_{1} \operatorname{rest} r \; \theta \; \text{end} \\ \widetilde{\mathcal{E}} \vdash_{x} m : \operatorname{rease}_{comp}(M_{1}) & \widetilde{z} \; \operatorname{ferkin} \; n \; \widetilde{E} \\ Vf \in \operatorname{pros}(S_{1}), \; (\mathcal{E}, \operatorname{module} \widetilde{z} : \operatorname{abs}_{cper} \widetilde{M} \vdash (T) \; m(\overline{z}) \; f \; (T \mid I_{f})) \\ Vf \in \operatorname{pros}(S_{1}), \; \mathcal{I} \; \operatorname{comp} (J \mid f) \\ \widetilde{\mathcal{E}}, \; \operatorname{module} x = n : \operatorname{abs}_{cper} : M_{1} \vdash (\phi) \; x \; (\psi \mid I_{x}) \\ \widetilde{\mathcal{E}}, \; \operatorname{module} x = n : \operatorname{abs} t \mid (\phi) \; x \; (\psi \mid I_{x}) \end{array}$

where:

 $T_{ins} = \{G \mapsto t_s[G] + \sum_{f \in procs(S_f)} t_s[x, f] \cdot t_f[G]\}$

 $\begin{array}{ll} t_{f} \leq_{\operatorname{compl}} \theta[f] &= \forall z_{0} \in \vec{z}, \forall g \in \operatorname{procs}(\vec{\mathsf{M}}[z_{0}]), t_{f}[z_{0}.g] \leq \theta[f][z_{0}.g] \land \\ t_{f}[\operatorname{conc}] + \sum_{\substack{\mathsf{A} \in \operatorname{And}(\mathcal{E}) \\ \mathsf{A} \in \operatorname{procs}_{f}(\mathsf{A})}} t_{f}[\mathsf{A}.h] \cdot \operatorname{int}_{\mathcal{E}}(\mathsf{A}.h) \leq \theta[f][\operatorname{int}_{\mathcal{E}}(\mathcal{E})] \land \\ \end{array}$

Conventions: $intr_{\mathcal{E}}(A, h)$ is the intr field in the complexity restriction of the abstract module procedure A, h in \mathcal{E} .

Figure 23: Instantiation rule for cost judgment.

Module path typing $\Gamma \vdash p : M$

NAME	Compat		
$\Gamma(p) = _: M$	$\Gamma \vdash p : sig S_1; module x : M; S_2 restr \theta end$		
$\Gamma \vdash p:M$	Γ ⊢ p.x : M		

 $\Gamma \vdash p : func(x : M') M = \Gamma \vdash p' : M'$ $\Gamma \vdash p(p') : M[x \mapsto mem_{\tau}(p')]$

Module expression typing $\Gamma \vdash_0 m : M$.

We omit the rules $\Gamma \vdash M$ to check that a module signature M is well-formed.

$\Gamma \vdash p_a : M$	STRUCT $\Gamma \vdash_{\mathbf{p}, \theta} \text{st} : S$		
$\Gamma \vdash_p p_a : M$	$\Gamma \vdash_{p} struct st end : sig S restr \theta end$		
FUNC		Sun	
$\Gamma \vdash M_0$	Γ(x)f undef	$\Gamma \vdash_p m : M_0$	
Γ , module $x = ab$	⊢ M ₀ <: M		
$\Gamma \vdash_n func(x : N)$	$\Gamma \vdash_n m : M$		

Module structure typing $\Gamma \vdash_{\Gamma, \theta} st : S$.

 $\begin{array}{l} \mbox{ProcDuct} & \mbox{body} = \{ \mbox{ var} (\vec{n}: \vec{\eta}); \mbox{ s}; \mbox{ return } r \ \} \\ \vec{v}, \vec{n}, \mbox{ fresh} in \ \Gamma & \ \Gamma_f = \Gamma, \mbox{ var} \vec{n}: \vec{\tau}, \ \mbox{ var} \vec{n}: \vec{\tau} \\ \Gamma(p, f) \mbox{ var} (\vec{n}: \vec{\tau}) \rightarrow r; \ \Gamma \ \mbox{ body} \ \mbox{ body} \ \mbox{ body} \ \mbox{ body} \\ \vec{\Gamma} \ \mbox{ p}, \mbox{ p} \ \mbox{ p} \ \mbox{ return } r \ \mbox{ s} \ \mbox{ body} \ \mbox{ body} \ \mbox{ body} \ \mbox{ body} \ \mbox{ s} \ \mbox{ body} \ \mbox{ s} \ \mbox{ s} \ \mbox{ s} \ \mbox{ s} \ \mbox{ return } r \ \mbox{ s} \ \mbox{ return } \ \mbox{ s} \ \mbox{ s$

 $\Gamma \vdash_{p, \emptyset} (\text{module } x = m; \ \text{st}) : (\text{module } x : M; \ S)$

STRUCTEMI

Tto etc

Environments typing ⊢ &

ENVEMP	EnvSp $\vdash \mathcal{E}$	ε+δ	$\mathcal{E}_{\text{NVVAR}} = \mathcal{E}(v) j_{\text{undef}}$	
F #	$+ \mathcal{E}, \delta$		$\mathcal{E} \vdash \text{var } v : r$	
NVMOD		EnvAss		
S⊦xm∶M	$\mathcal{E}(\mathbf{x})_{t=undef}$	$\mathcal{E} \vdash M_{i}$	E(x) ± undef	
£ ⊢ (modul	$e x = m \cdot M$	$E \ge (mo)$	fulle $x = abs_{W} \cdot M$	

Figure 13: Core typing rules.

- Hoare logic for cost + typing rules for module restrictions.
- **Rules** handling abstract code are the most interesting.

Implementation in EASYCRYPT

EASYCRYPT

A proof assistant to verify cryptographic proofs. It relies on:

- general purpose higher-order ambient logic.
- probabilistic relational Hoare logic (pRHL).
- powerful module system.

Many advanced existing case studies: AWS KMS, SHA3, ...

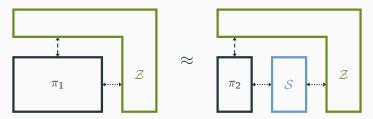
- Hoare logic for cost has been **implemented** in **EASYCRYPT**.
- Integrated in EASYCRYPT ambient higher-order logic.
 ⇒ meaningful existential quantification over abstract code (e.g. ∀∃ statements).
- Established the complexity of classical examples: BR93, Hashed El-Gamal, Cramer-Shoup.

Application: Universal Composability in EASYCRYPT

- UC is a general framework providing strong security guarantees
- Fundamentals properties: transitivity and composability. ⇒ allow for modular and composable proofs.

Universal Composability

←---→ I/O ← Backdoor

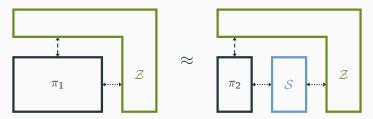


 $\exists \mathcal{S} \in \mathsf{Sim}, \forall \mathcal{Z} \in \mathsf{Env},$

 $|\Pr[\mathcal{Z}(\pi_1) : \operatorname{true}] - \Pr[\mathcal{Z}(\langle \pi_2 \circ \mathcal{S} \rangle) : \operatorname{true}]| \leq \epsilon$

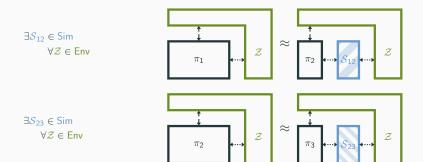
Universal Composability

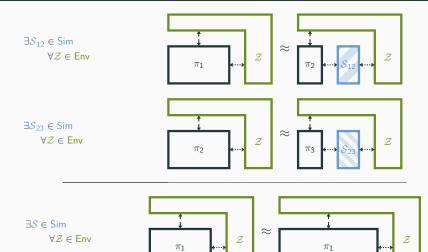
←---→ I/O ← Backdoor

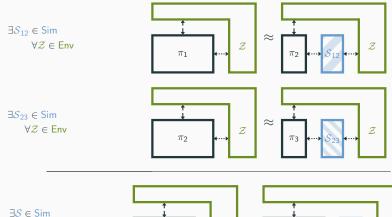


 $\exists S \in \mathsf{Sim}[c_{\mathsf{sim}}], \forall Z \in \mathsf{Env}[c_{\mathsf{env}}], \\ | \Pr[\mathcal{Z}(\pi_1) : \mathsf{true}] - \Pr[\mathcal{Z}(\langle \pi_2 \circ S \rangle) : \mathsf{true}] | \le \epsilon$

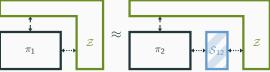
Z is the adversary: its complexity must be bounded.
if S's complexity is unbounded, UC key theorems become useless.

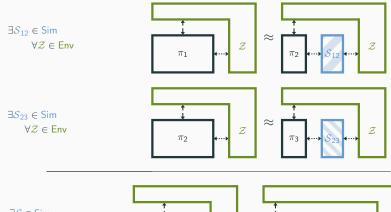




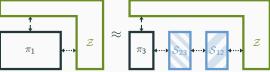


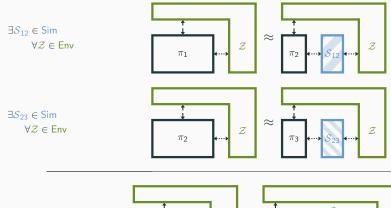
 $\forall \mathcal{Z} \in \mathsf{Env}$



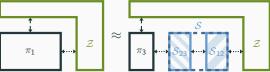


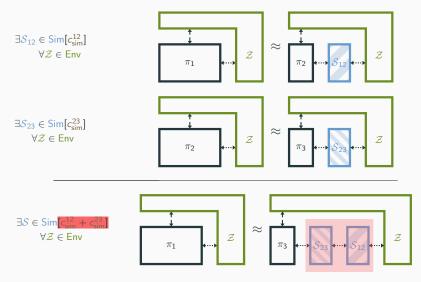
 $\exists \mathcal{S} \in \mathsf{Sim} \\ \forall \mathcal{Z} \in \mathsf{Env} \end{cases}$



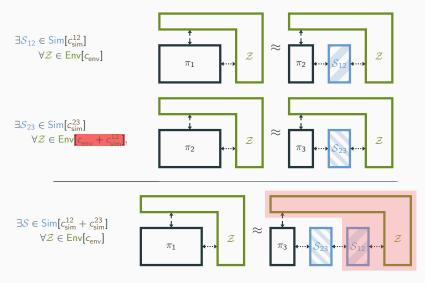


 $\exists \mathcal{S} \in \mathsf{Sim} \\ \forall \mathcal{Z} \in \mathsf{Env} \end{cases}$

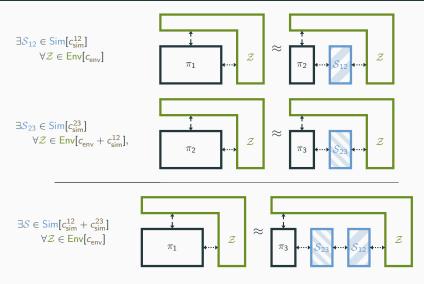




 \Rightarrow precise complexity bounds are crucial here.



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- UC formalization in EASYCRYPT, with fully mechanized general UC theorems (transitivity, composability).
- Our formalization exploits EASYCRYPT machinery:
 - module restrictions for complexity/memory footprint constraints;
 - **message passing** done through **procedure calls**.
 - \Rightarrow simple and usable formalism.

- Diffie-Hellman UC-emulates a Key-Exchange ideal functionality, assuming DDH.
- One-Time Pad+Key-Exchange UC-emulates a Secure Channel ideal functionality.

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- One-Time Pad+Key-Exchange UC-emulates a Secure Channel ideal functionality.
- Diffie-Hellman+One-Time Pad UC-emulates a one-shot Secure Channel ideal functionality, assuming DDH.
- Final security statements with precise probability and complexity bounds.

Conclusion

- Designed a Hoare logic for worst-case complexity upper-bounds.
- Implemented in EASYCRYPT, embedded in its ambient higher-order logic.
 - ⇒ fully mechanized and composable crypto. reductions.
- First formalization of EASYCRYPT module system. (of independent interest)
- Main application: UC formalization in EASYCRYPT. Key results (transitivity, composability) and examples (DH+OTP) are fully mechanized.

Thank you for your attention.