

SQUIRREL, an Interactive Prover for Protocol Verification in the Computational Model

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October 28, 2020

Security Protocols

Distributed programs which aim at providing some **security** properties.



Security Attacks

Attacks against security protocols can be very **damageable**, e.g. theft or privacy breach.

⇒ We need to check that protocols are secure:

formal methods allow to do that, with strong guarantees.

Verification of Security Protocols

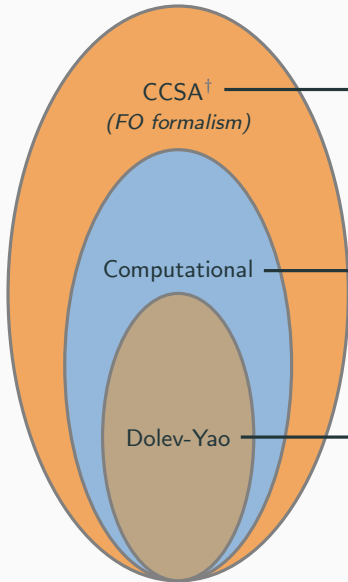
The goal is to completely rule-out classes of attacks.

$$\forall \mathcal{A} \in \mathcal{C}, \quad (\mathcal{A} \parallel P) \models \phi$$

Attacker Class

What is the class \mathcal{C} of attackers?

Attacker Classes from the Literature



Adversary: any **arbitrary** function \mathcal{A} that satisfies some **axioms**, i.e. $\mathcal{A} \models Ax$
Defined by what he **cannot** do, e.g.:
 $\{m_0\}_{pk} \sim \{m_1\}_{pk}$ (if $\text{len}(m_0) = \text{len}(m_1)$)
✓ Strong security ✓ Good automation

Adversary: any **PPT** function \mathcal{A} models a real-world attacked.
✓ Strong security ✗ Limited automation

Adversary: **fixed** set of rules \mathcal{E}
Defined by what he **can** do.
E.g. $\text{dec}(\{x\}_{pk}, sk) \rightarrow x$
✗ Reduced security ✓ Good automation

† *Computationally Complete Symbolic Attacker*

[BC12], [CLCS14]

- First framework, **only for reachability properties**.
- A tool implementing a decision procedure, tested on a few protocols for a small number of sessions.

[BC14], [CK17]

- New framework, both for **reachability and equivalence** properties.
- Framework allows to do **manual** proofs, only for a **bounded number** of sessions.

Our Contributions (under submission, S&P).

Contribution 2:

An interactive prover, SQUIRREL, to **mechanize proofs**.

Manual proofs, only for a bounded number of sessions.

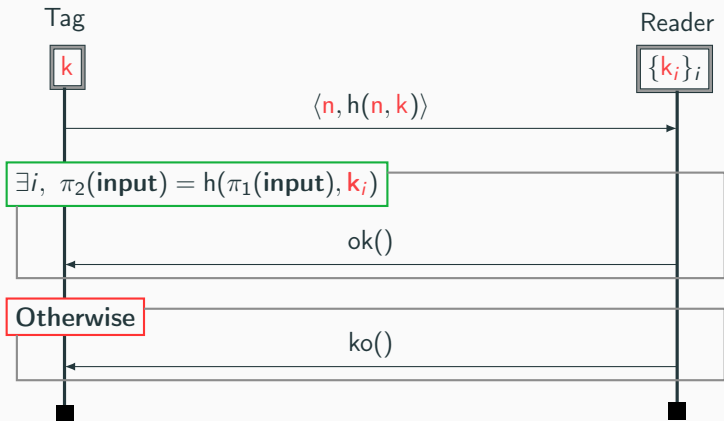
Contribution 1:

A theoretical framework (a **meta-logic**) to express and prove security properties (reachability and equivalence) for an **arbitrary number of sessions**.

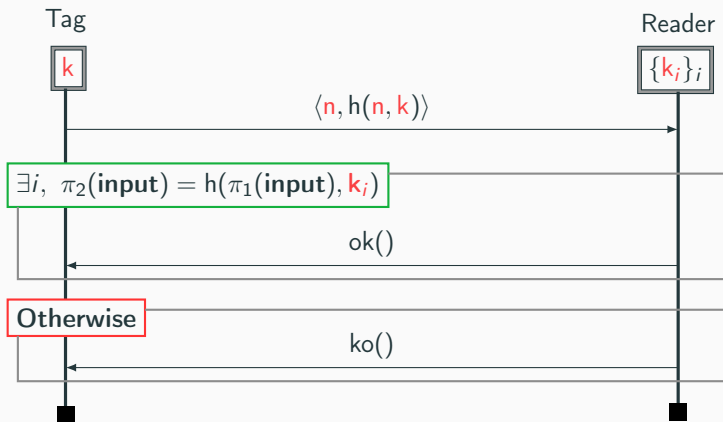
- 1 The Base logic: CCSA
- 2 The Meta-Logic
- 3 An Interactive Theorem Prover, **SQUIRREL**

The Base logic: CCSA

Basic Hash Protocol



Basic Hash Protocol



To formally model this protocol's security, we need to model:

- messages, i.e. distributions over bit-strings \Rightarrow terms
- security properties (reachability or equivalence) \Rightarrow formulas

Bana-Comon Approach: Messages

We model *protocol messages* using **terms** built upon:

- **names** \mathcal{N} , e.g. n_A, n_B , for random samplings (including keys).
- **function symbols** \mathcal{F} for protocol functions, e.g.:

$h(_, _), \langle _, _ \rangle, \pi_i(_), \text{ok}(), \text{if_then_else_}, \text{eq}(_, _)$

- **function symbols** \mathcal{G} for adversarial computations, e.g.:

$\text{att}(_)$

- **variables** $x \in \mathcal{X}$.

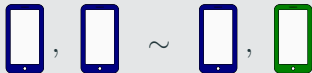
CCSA Approach: Formulas

We model security properties using **formulas**, which are built using a predicate \sim of arbitrary arity.

$$\phi ::= \phi \vee \phi \mid \neg \phi \mid \exists x, \phi \mid \vec{u} \sim \vec{v}$$

Basic Hash Unlinkability (weak version)

Weak unlinkability for two tags and **two sessions**:



$$\langle n, h(n, k_0) \rangle, \langle n', h(n', k_0) \rangle \sim \langle n, h(n, k_0) \rangle, \langle n', h(n', k_1) \rangle$$

Models of our logic are called computational models, where a computational model \mathbb{M} interprets:

- terms as **PPT Turing machines**:
 - names as independent random samplings;
 - function symbols as deterministic machines.
- \sim as **computational indistinguishability**.

Validity

We note $\mathbb{M} \models \phi$ when the base logic formula holds in the computational model \mathbb{M} .

A base logic formula ϕ is **valid** if $\mathbb{M} \models \phi$ for every \mathbb{M} .

CCSA Approach: Axioms

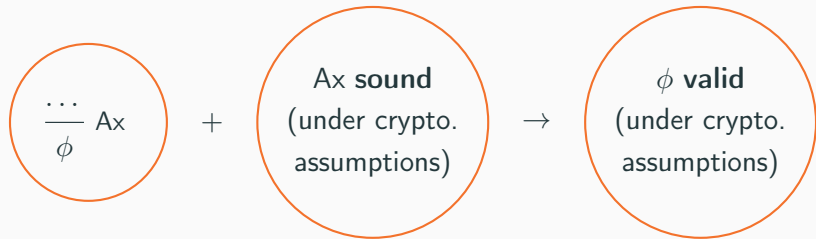
To prove that ϕ is **valid**, we **axiomatize** what the adversary **cannot do**. We restrict the models \mathbb{M} using axioms Ax:

- **structural axioms**;
- **implementation axioms**, e.g. functional properties;
- **cryptographic axioms**, e.g. EUF-CMA, PRF.

Axioms are given as **inference rules**.

$$\frac{\Delta_1 \vdash \phi_1 \dots \Delta_n \vdash \phi_n}{\Delta \vdash \phi}$$

CCSA Approach: Axioms



CCSA Approach: Examples of Axioms

DUP

$$\frac{\Delta \vdash \vec{u}, s \sim \vec{v}, t}{\Delta \vdash \vec{u}, s, s \sim \vec{v}, t, t}$$

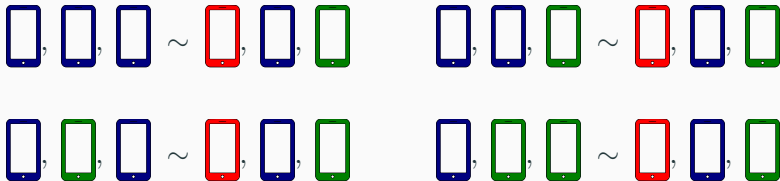
PRF

$$\frac{\begin{array}{l} \text{if } \text{HFresh}^k(t; \vec{u}, t) \\ \Delta \vdash \vec{u}, \text{ then } n \quad \sim \vec{v} \\ \text{else } h(t, k) \end{array}}{\Delta \vdash \vec{u}, h(t, k) \sim \vec{v}}$$

when $\text{SC}^{n,k}(t, \vec{u})$

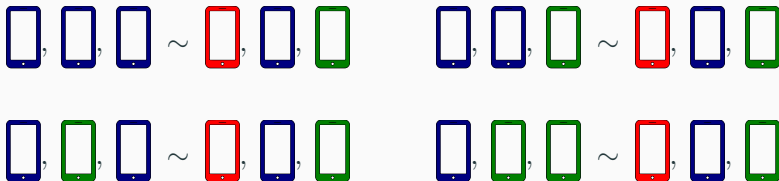
CCSA Approach: Limitations

Weak unlinkability for two tags A, B with **three sessions**:



CCSA Approach: Limitations

Weak unlinkability for two tags A, B with **three sessions**:



We have to **manually prove all these equivalences!**

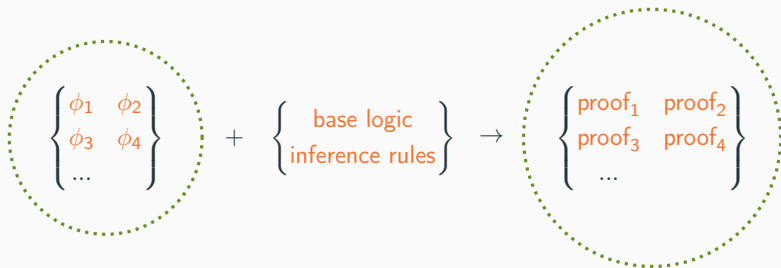
- **Limited guarantees:** only proved for three sessions.
- Lots of **redundant** reasoning between cases.

Moreover, to prove security for a **fixed** n , e.g. 3, we often need to understand why security holds **for any** n .

The Meta-Logic

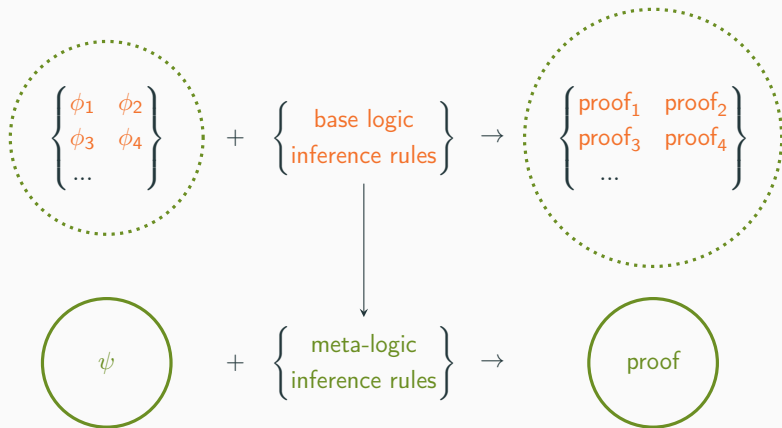
Solution: a Meta-Logic

Goal: prove security for any interleaving, in a single proof.



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Solution: a Meta-Logic

$$\left\{ \begin{array}{cc} \phi_1 & \phi_2 \\ \phi_3 & \phi_4 \\ \dots & \end{array} \right\} = \left\{ \begin{array}{c} \boxed{\phantom{A_{i_1}}}, \dots, \boxed{\phantom{A_{i_n}}} \\ \sim \\ \boxed{}, \dots, \boxed{} \end{array} \mid \begin{array}{l} \text{for any } n \in \mathbb{N} \text{ and} \\ \left(\boxed{\phantom{A_{ij}}} \in \{ \boxed{\phantom{A_{ij}}}, \boxed{\phantom{A_{ij}}} \} \right)_{1 \leq j \leq n} \end{array} \right\}$$

Solution: a Meta-Logic

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$$\psi = \forall \mathcal{T}, \text{ frame}@_{\mathcal{T}} \sim \text{frame}^u@_{\mathcal{T}}$$

Protocols as a Set of Actions

To do this, we need a **formal description of protocols**.

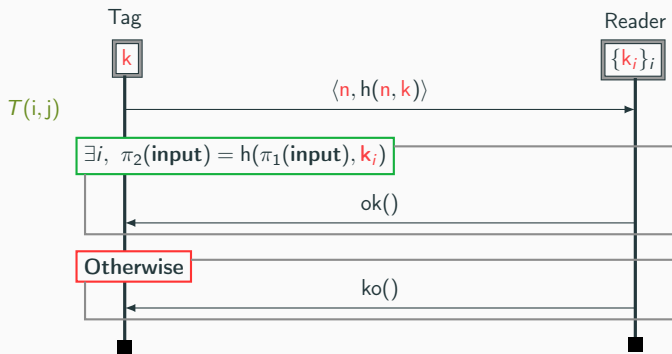
An Action is:

- a **condition**,
- and an **output** message.

A Protocol is:

- a finite set of **actions**,
- equipped with a **dependency relation** to constrain the execution order of actions.

Protocols as a Set of Actions

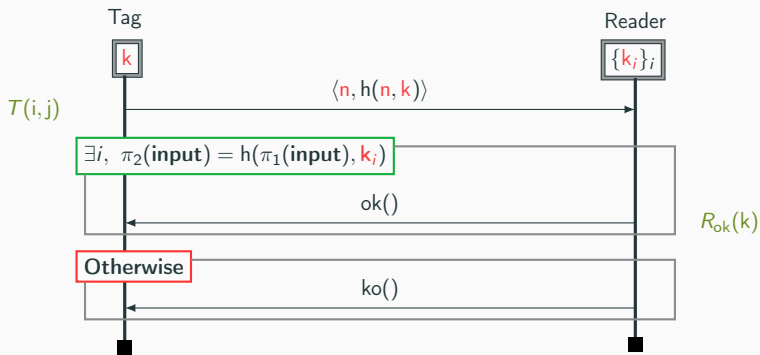


Action $T(i, j)$: session j of the tag i

Condition: true

Output: $\langle n[i, j], h(n[i, j], k[i]) \rangle$

Protocols as a Set of Actions

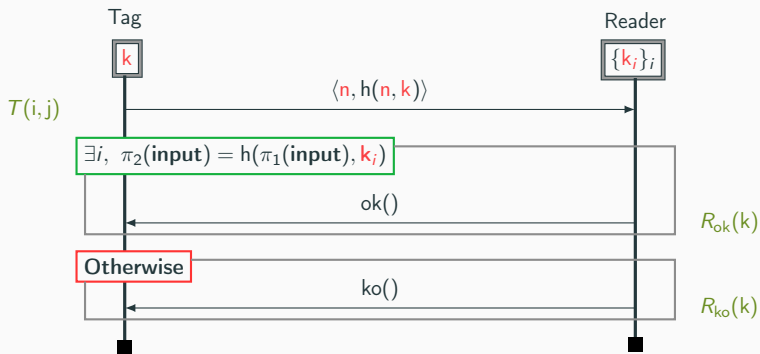


Action $R_{ok}[k]$: session k of the reader, accept

Condition: $\exists i, \pi_2(\text{input}@R_{ok}[k]) = h(\pi_1(\text{input}@R_{ok}[k]), k[i])$

Output: ok()

Protocols as a Set of Actions

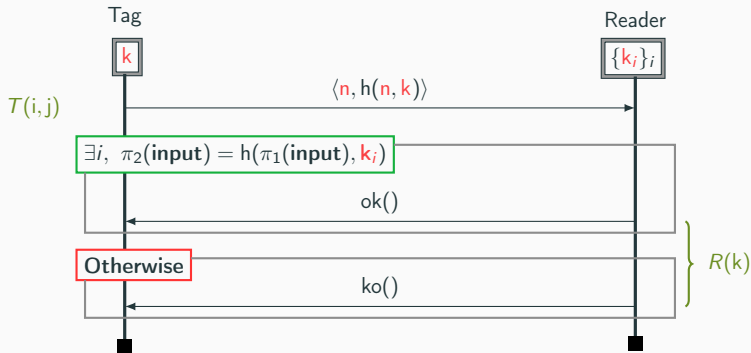


Action $R_{\text{ko}}[k]$: session k of the reader, reject

Condition: $\neg(\exists i, \pi_2(\text{input}@R_{\text{ko}}[k]) = h(\pi_1(\text{input}@R_{\text{ko}}[k]), k[i]))$

Output: $\text{ko}()$

Protocols as a Set of Actions



Bonus Action $R[k]$: session k of the reader, accept or reject

Condition: true

Output: find i s.t. $\pi_2(\text{input}@R[k]) = h(\pi_1(\text{input}@R[k]), k[i])$ then $\text{ok}()$
else $\text{ko}()$

Extension of the base logic with:

- **index variables** \mathcal{I} , to represent session numbers, agent numbers, etc: i_1, \dots, i_n
- **indexed names**, e.g. $n[i_1, \dots, i_k]$
- **timestamps variables** \mathcal{T} **and terms**, to quantify over all possible instants of a trace: τ or $T(i, j)$.
- **macros** $\text{cond}@_{\mathcal{T}}$, $\text{input}@_{\mathcal{T}}$, $\text{output}@_{\mathcal{T}}$ to talk about the condition, input and output of the action at instant τ
- **quantifications** over timestamps and indices.

Meta-Logic: Translation to the Base Logic

A meta-formula ψ represents a set of base-formulas. Roughly:

$$\psi \text{ represents } \left\{ (\psi)^{\mathbb{T}} \mid \text{for any "trace" } \mathbb{T} \right\}$$

Trace Model \mathbb{T}

A trace model \mathbb{T} is a tuple $(\mathcal{D}_{\mathcal{I}}, \mathcal{D}_{\mathcal{T}}, <_{\mathcal{T}}, \sigma_{\mathcal{I}}, \sigma_{\mathcal{T}})$:

- $\mathcal{D}_{\mathcal{I}}, \mathcal{D}_{\mathcal{T}}$ are index and timestamp domains;
- $<_{\mathcal{T}}$ is a total ordering on $\mathcal{D}_{\mathcal{T}}$;
- $\sigma_{\mathcal{I}} : \mathcal{I} \rightarrow \mathcal{D}_{\mathcal{I}}$ interprets index variables;
- $\sigma_{\mathcal{T}} : \mathcal{T} \rightarrow \mathcal{D}_{\mathcal{T}}$ interprets timestamp variables.

Translation function $(_)^{\mathbb{T}}$ from meta-formulas and terms to base-formulas and terms.

Meta-Logic: Translation to the Base Logic, an Example

Let's consider a trace of the Basic Hash protocol: $T[3, 1].R_{ok}[2].T[3, 2]$.

- $\mathcal{D}_{\mathcal{I}} = \{1, 2, 3\}$.
- $\sigma_{\mathcal{I}} = \{i \mapsto 3, j \mapsto 1, j' \mapsto 2, k \mapsto 2\}$

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- $(n[i, j])^{\mathbb{T}} := n_{3,1}$
- $(n[i, j'])^{\mathbb{T}} := n_{3,2}$
- $(\text{output}@T[i, j])^{\mathbb{T}} := \langle n_{3,1}, h(n_{3,1}, k_3) \rangle$

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- $(\text{output}@T[i, j])^{\mathbb{T}} := \langle n_{3,1}, h(n_{3,1}, k_3) \rangle$
- $(\text{cond}@R_{ok}[k])^{\mathbb{T}}$
 - $:= (\exists i, \pi_2(\text{input}@R[k]) = h(\pi_1(\text{input}@R[k]), k[i]))^{\mathbb{T}}$
 - $:= \pi_2(\text{att}(\dots)) = h(\pi_1(\text{att}(\dots)), k_1)$
 - $\dot{\vee} \pi_2(\text{att}(\dots)) = h(\pi_1(\text{att}(\dots)), k_2)$
 - $\dot{\vee} \pi_2(\text{att}(\dots)) = h(\pi_1(\text{att}(\dots)), k_3)$

Meta-Logic: Translation to the Base Logic, Some Details

Selected (simplified) rules:

$$(f(t_1, \dots, t_n))^{\mathbb{T}} = f((t_1)^{\mathbb{T}}, \dots, (t_n)^{\mathbb{T}})$$

$$(\exists i. \phi)^{\mathbb{T}} = \bigvee_{k \in \mathcal{D}_{\mathcal{I}}} (\phi)^{\mathbb{T}\{i \mapsto k\}}$$

$$(\forall \tau. \phi)^{\mathbb{T}} = \bigwedge_{v \in \mathcal{D}_{\mathcal{T}}} (\phi)^{\mathbb{T}\{\tau \mapsto v\}}$$

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and for macros:

$$(\text{output@}\tau)^{\mathbb{T}} = \textit{specified by the protocol}$$

$$(\text{cond@}\tau)^{\mathbb{T}} = \textit{specified by the protocol}$$

$$(\text{input@}\tau)^{\mathbb{T}} = \text{att}((\text{frame@pred}(\tau))^{\mathbb{T}})$$

$$(\text{frame@}\tau)^{\mathbb{T}} \approx \langle (\text{frame@pred}(\tau))^{\mathbb{T}}, (\text{output@}\tau)^{\mathbb{T}} \rangle$$

Validity: Meta-Logic

We note $\mathbb{T}, \mathbb{M} \models \psi$ when the **meta-logic** formula ψ holds in trace model \mathbb{T} and in the computational model \mathbb{M} :

$$\mathbb{T}, \mathbb{M} \models \psi \quad \text{iff.} \quad \mathbb{M} \models (\psi)^{\mathbb{T}}$$

A **meta-logic** formula ψ is **valid** if $(\psi)^{\mathbb{T}}$ is valid for every \mathbb{T} .

Meta-Logic: Lifting Axioms

Base logic rule

$$\frac{\text{DUP} \quad \Delta \vdash \vec{u}, s \sim \vec{v}, t}{\Delta \vdash \vec{u}, s, s \sim \vec{v}, t, t}$$

Meta-logic rule

$$\frac{\text{DUP} \quad \Delta \vdash \vec{u}, s \sim \vec{v}, t}{\Delta \vdash \vec{u}, s, s \sim \vec{v}, t, t}$$

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Base logic rule

$$\text{PRF} \frac{\Delta \vdash \vec{u}, \begin{array}{l} \text{if } \text{HFresh}^k(t; \vec{u}, t) \\ \text{then } n \\ \text{else } h(t, k) \end{array} \sim \vec{v}}{\Delta \vdash \vec{u}, h(t, k) \sim \vec{v}}$$

when $\text{SC}^{n,k}(t, \vec{u})$

Meta-logic rule

$$\text{PRF} \frac{\Delta \vdash \vec{u}, \begin{array}{l} \text{if } \text{HFresh}_{\mathcal{P}}^{k[\vec{i}]}(t; \vec{u}, t) \\ \text{then } n \\ \text{else } h(t, k[\vec{i}]) \end{array} \sim \vec{v}}{\Delta \vdash \vec{u}, h(t, k[\vec{i}]) \sim \vec{v}}$$

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when $\text{SC}^{n,k}(t, \vec{u})$

$\text{HFresh}^k(t; \vec{u}, t)$ and $\text{SC}^{n,k}(t, \vec{u})$
can be checked/computed
syntactically.

Meta-logic rule

$$\text{PRF} \frac{\Delta \vdash \vec{u}, \begin{array}{l} \text{if } \text{HFresh}_{\mathcal{P}}^{k[\vec{i}]}(t; \vec{u}, t) \\ \text{then } n \\ \text{else } h(t, k[\vec{i}]) \end{array} \sim \vec{v}}{\Delta \vdash \vec{u}, h(t, k[\vec{i}]) \sim \vec{v}}$$

when $\text{SC}_{\mathcal{P}}^{n,k[\vec{i}]}(t, \vec{u})$

$\text{HFresh}_{\mathcal{P}}^{k[\vec{i}]}(t; \vec{u}, t)$ and $\text{SC}_{\mathcal{P}}^{n,k[\vec{i}]}(t, \vec{u})$
need to be checked/computed for:
- **direct** occurrences (syntactically),
- and **indirect** occurrences (any action
of the protocol).

Meta-Logic: Basic Hash Protocol Security

Using the **meta-logic inference rules**, we are able to derive all at once **a family of base logic formulas**.

(Do you recall the long list of equivalences shown previously?)

It starts like this:

$$\frac{\frac{\dots}{\tau = T[i,j], \dots \vdash \dots} \quad \frac{\dots}{\tau = R_{ok}[k], \dots \vdash \dots} \quad \frac{\dots}{\tau = R_{ko}[k], \dots \vdash \dots}}{\text{frame}@pred(\tau) \sim \text{frame}^u@pred(\tau) \vdash \text{frame}@_{\tau} \sim \text{frame}^u@_{\tau}} \quad \text{Ind}} \frac{}{\vdash \text{frame}@_{\tau} \sim \text{frame}^u@_{\tau}}$$

An Interactive Theorem Prover, SQUIRREL

- The **input language** is a variant of the applied-pi calculus.
- We have implemented:
 - the **translation** of the specification of the protocol from this input language to actions,
 - **proof tactics**, corresponding to inference rules,
 - **automated reasoning** to ease the proof effort.
- The **user** interacts with the prover by **calling tactics** to derive formulas step by step.

Case Studies

Protocol	Crypto. assumptions	Security properties
Basic Hash	PRF, EUF-CMA	Authentication & Unlinkability
Hash Lock	PRF, EUF-CMA	Authentication & Unlinkability
LAK (pairs)	PRF, EUF-CMA	Authentication & Unlinkability
MW	PRF, EUF-CMA, XOR	Authentication & Unlinkability
Feldhofer	CCA ₁ , PRF, EUF-CMA	Authentication & Unlinkability
Private Auth.	CCA ₁ , EUF-CMA, ENC-KP	Anonymity
Signed DDH	EUF-CMA, DDH	Authentication & Strong Secrecy
Additional case studies, using the composition framework from [CJS20]		
Signed DDH	EUF-CMA, DDH	Authentication & Strong Secrecy
SSH (fwd agent)	EUF-CMA, DDH	Authentication & Strong Secrecy

[demo]

Conclusion

Our contribution

- **Meta-logic** built on the **CCSA model**.
- Set of **meta-logic inference rules** for proving reachability and equivalence properties.
- **SQUIRREL**, an interactive prover **implementing** these inference rules, used on various **case studies**.

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Current and future work

- Extend support to **stateful** and **more complex** protocols.
- More **proof automation**.

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- More **proof automation**.

Thank you for your attention!

References



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